## Algebraic Geometry for Theoretical Computer Science Assignment 9

Lecturer: Gil Cohen Hand in date: January 8, 2015

**Instructions:** Please write your solutions in LaTeX / Word or exquisite handwriting. Submission can be done individually or in pairs.

Consider the function field  $\mathbb{F}_4(x,y)/\mathbb{F}_4$  given by

$$y^3 = \frac{x^3}{x^2 + x + 1} \,.$$

- 1. Find all the rational places of this function field. Please use a diagram as shown in class, that describes which place is over which and what are the ramification indices and relative degree of the extensions.
- 2. What are the principal divisors of x and y?